

1	(i)	(A) $P(X = 10) = P(5 \text{ then } 5) = 0.4 \times 0.25 = 0.1$	B1 ANSWER GIVEN	[1]
		(B) $P(X = 30) = P(10 \text{ and } 20) = 0.4 \times 0.25 + 0.2 \times 0.5 = 0.2$	M1 for full calculation A1 ANSWER GIVEN	[2]
	(ii)	$E(X) = 10 \times 0.1 + 15 \times 0.4 + 20 \times 0.1 + 25 \times 0.2 + 30 \times 0.2 = 20$ $E(X^2) = 100 \times 0.1 + 225 \times 0.4 + 400 \times 0.1 + 625 \times 0.2 + 900 \times 0.2 = 445$ $\text{Var}(X) = 445 - 20^2 = 45$	M1 for $\sum rp$ (at least 3 terms correct) A1 CAO M1 for $\sum r^2 p$ (at least 3 terms correct) M1 dep for – their $E(X)^2$ A1 FT their $E(X)$ provided $\text{Var}(X) >$	[5]
			TOTAL	[8]

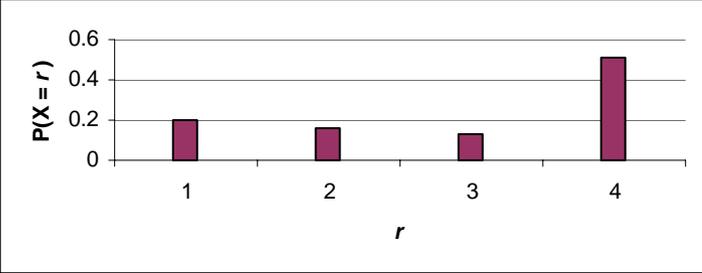
2	(i)	$\text{Mean} = \frac{126}{12} = 10.5$ $S_{xx} = 1582 - \frac{126^2}{12} = 259$ $s = \sqrt{\frac{259}{11}} = 4.85$	B1 for mean M1 for attempt at S_{xx} A1 CAO	3
	(ii)	New mean = $500 + 100 \times 10.5 = 1550$ New $s = 100 \times 4.85 = 485$	B1 <u>ANSWER GIVEN</u> M1A1FT	3
	(iii)	On average Marlene sells more cars than Dwayne. Marlene has less variation in monthly sales than Dwayne.	E1 E1FT	2
			TOTAL	8

3 (i)	$E(X) = 25$ because the distribution is symmetrical. Allow correct calculation of Σrp	E1 <u>ANSWER GIVEN</u>	1
(ii)	$E(X^2) = 10^2 \times 0.2 + 20^2 \times 0.3 + 30^2 \times 0.3 + 40^2 \times 0.2 = 730$ $\text{Var}(X) = 730 - 25^2 = 105$	M1 for $\Sigma r^2 p$ (at least 3 terms correct) M1dep for $- 25^2$ A1 CAO	3
		TOTAL	

4 (i)	$p = 0.55$	B1 cao	1
(ii)	$E(X) = 0 \times 0.55 + 1 \times 0.1 + 2 \times 0.05 + 3 \times 0.05 + 4 \times 0.25 = 1.35$ $E(X^2) = 0 \times 0.55 + 1 \times 0.1 + 4 \times 0.05 + 9 \times 0.05 + 16 \times 0.25 = 0 + 0.1 + 0.2 + 0.45 + 4 = (4.75)$ $\text{Var}(X) = \text{'their'} 4.75 - 1.35^2 = 2.9275 \text{ awfw } (2.9275 - 2.93)$	M1 for Σrp (at least 3 non zero terms correct) A1 CAO (no 'n' or 'n-1' divisors) M1 for $\Sigma r^2 p$ (at least 3 non zero terms correct) M1dep for – their $E(X)^2$ provided $\text{Var}(X) > 0$ A1 cao (no 'n' or 'n-1' divisors)	5
(iii)	$P(\text{At least 2 both times}) = (0.05 + 0.05 + 0.25)^2 = 0.1225 \text{ o.e.}$	M1 for $(0.05 + 0.05 + 0.25)^2$ or 0.35^2 seen A1cao: awfw (0.1225 - 0.123) or 49/400	2
		TOTAL	8

5 (i)	$X \sim B(50, 0.03)$		
	<p>(A) $P(X = 1) = \binom{50}{1} \times 0.03 \times 0.97^{49} = 0.3372$</p> <p>(B) $P(X = 0) = 0.97^{50} = 0.2181$</p> <p>$P(X > 1) = 1 - 0.2181 - 0.3372 = 0.4447$</p>	<p>M1 0.03×0.97^{49} or $0.0067(4)....$</p> <p>M1 $\binom{50}{1} \times pq^{49}$ (p+q =1)</p> <p>A1 CAO (awfw 0.337 to 0.3372) or 0.34(2s.f.) or 0.34(2d.p.) but not just 0.34</p> <p>B1 for 0.97^{50} or 0.2181 (awfw 0.218 to 0.2181)</p> <p>M1 for $1 - ('their' p(X = 0) + 'their' p(X = 1))$ must have both probabilities A1 CAO (awfw 0.4447 to 0.445)</p>	3 3
(ii)	Expected number = $np = 240 \times 0.3372 = 80.88 - 80.93 = (81)$ <i>Condone $240 \times 0.34 = 81.6 = (82)$ but for M1 A1f.t.</i>	M1 for $240 \times \text{prob (A)}$ A1FT	2
		TOTAL	8

6 (i)	Mean = 7.35 (or better)	B2cao $\sum fx = 323.5$	
	Standard deviation: 3.69 – 3.70 (awfw)	B2cao $\sum fx^2 = 2964.25$	
	Allow $s^2 = 13.62$ to 13.68	(B1) for variance s.o.i.o	
	Allow rmsd = 3.64 – 3.66 (awfw)	(B1) for rmsd	
	After B0, B0 scored then if at least 4 correct mid-points seen or used. {1.5, 4, 6, 8.5, 15}	(B1) mid-points	
	Attempt of their mean = $\frac{\sum fx}{44}$, with $301 \leq fx \leq 346$ and fx strictly from mid-points not class widths or top/lower boundaries.	(B1) $6.84 \leq \text{mean} \leq 7.86$	4
(ii)	Upper limit = $7.35 + 2 \times 3.69 = 14.73$ or 'their sensible mean' + $2 \times$ 'their sensible s.d.'	M1 (with s.d. < mean)	
	So there could be one or more outliers	E1dep on B2, B2 earned and comment	2
		TOTAL	6

7 (i)	$E(X) = 1 \times 0.2 + 2 \times 0.16 + 3 \times 0.128 + 4 \times 0.512 = 2.952$ <p>Division by 4 or other spurious value at end loses A mark</p> $E(X^2) = 1 \times 0.2 + 4 \times 0.16 + 9 \times 0.128 + 16 \times 0.512 = 10.184$ $\text{Var}(X) = 10.184 - 2.952^2 = 1.47 \text{ (to 3 s.f.)}$	M1 for $\sum rp$ (at least 3 terms correct) A1 cao M1 for $\sum x^2p$ at least 3 terms correct M1 for $E(X^2) - E(X)^2$ Provided ans > 0 A1 FT their $E(X)$ but not a wrong $E(X^2)$	5										
(ii)	Expected cost = $2.952 \times \text{£}45000 = \text{£}133000$ (3sf)	B1 FT (no extra multiples / divisors introduced at this stage)	1										
(iii)	 <table border="1" data-bbox="284 832 986 1105"> <caption>Data for Bar Chart</caption> <thead> <tr> <th>r</th> <th>P(X=r)</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>0.2</td> </tr> <tr> <td>2</td> <td>0.16</td> </tr> <tr> <td>3</td> <td>0.128</td> </tr> <tr> <td>4</td> <td>0.512</td> </tr> </tbody> </table>	r	P(X=r)	1	0.2	2	0.16	3	0.128	4	0.512	G1 labelled linear scales G1 height of lines	2
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1	0.2												
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TOTAL			8										